

# Reinforced Concrete Structural Design and Analysis of a Single Cell Box Culvert Using Manual Method

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**ABSTRACT:** Box culvert is a hydraulic monolithic reinforced or non-reinforced concrete structure. <sup>1</sup>Culvert's classification by material is not limited to concrete but includes steel, aluminium, plastic, timber and high density polyethylene. Culverts permits the flow of water from through an inlet and an outlet under a normal roadway, railway. Because culverts main function is to accommodate and withstand various types of loads generated by traffic through human activities, soil fill, amongst others, this article is an exercise that deals with <sup>3</sup>holistic manual analysis and design of a single cell box culvert through the consideration of effects of earth pressures, surcharge pressures, hydrostatic and excess hydrostatic internal pressure, uniformly distributed permanent and live loads (of self-weight of the critical element/component and vehicular loads). Abstractedly, the dept of fill is 1.6m, the thickness of top, bottom, vertical side walls, the wing walls and apron slab floor are all uniformly 0.25m. The single cell culvert length is 6m and constructed across an asphalt surface finished roadway. BS5400 part 1, BS8110 part 1 (1985/1977), <sup>3</sup>Reynold and steelman's reinforced concrete designer's hand book are some of the codes and manuals used in the design and analysis of all the critical components to withstand maximum bending moment and shear force to specifications and standards. Summary of result of the manual design and analysis of the single cell culvert becomes main reinforcement bars: Y16mm@200 c/c for all components except for apron slab and distribution bars of Y12mm @ 200 c/c.

**Keywords:** HA, HB, Axle, top, slab, bottom, walls, apron, hydrostatic, reinforcement.

## I. INTRODUCTION

<sup>6</sup>A hydraulic structure that permits the flow of water from and through an inlet and an outlet which can be under a normal road, highway, railway or any flow obstructing elements/facility defines a culvert.

<sup>4</sup>Culverts are in many sizes and shapes such as box –like elliptical and circular round. Choice of shape and types is dependent on requirement such as limitations on upstream water, surface elevation, road way embankment height and requirement for hydraulic performance amongst others.

<sup>5</sup>In the structural design of culverts, load issues such as when the culvert is full of water and when the culvert is empty are considered. <sup>3</sup>Considered also are surcharge loads, earth pressures, hydrostatic and excess hydrostatic internal pressures. <sup>9</sup>Most important to be considered is the live load that will be passing through the culverts top (roof) slab. Other factors to be considered will include but not limited to the sizing (especially effective depth), <sup>5</sup>dispersal of load through earth fill, co-efficient of safety and earth pressure factors.

<sup>10,7</sup>The structural elements of a culvert such as top (roof) slab, bottom slab, the side vertical walls, wing walls, apron slab and head wall must be designed to withstand maximum bending moments and shear forces with adherence to relevant codes.

<sup>1</sup>The aim of this article or presentation is to showcase the design of the structural elements of a box culvert on the bases of structural requirement. The design of this box culvert will not include hydraulic consideration and requirement.

This presentation main objective is the suitable structural design of a single cell box culvert across Obibi drive road project off Alaka Avenue, Etevie community, Ozoro, Delta State through the determination of the total permanent and live loads acting on the structural components members of the box culvert to enable/facilitate the design and subsequent determination of reinforcement bars for the single cell box culvert.

<sup>4</sup>Culverts are in various geometric shapes and types classification that includes box culvert, pipe culvert, pipe arch culvert, bridge culvert and arch culvert.

Box culverts are preferred and more widely used because of its outstanding merits over

the other types of culverts. This is because amongst other of its merits, it can cope with budget flows, situations and available headroom is limited.<sup>1,5,7</sup> Box culverts can also be designed to suit a particular site situation by reducing or increasing its size easily than will be done in the case of other types of culvert.

The culvert will be analyzed with respect to critical loading conditions. The ultimate limit state will be with respect to the collapse of the culvert's structural elements while the serviceability limit state will be with or in respect to condition beyond which concern for loss of utility or for public concern over cracks and other serviceability concerns.

Loads on culvert includes;

- i. Permanent loads of self-weight (dead loads), the superimposed dead loads, the horizontal earth pressure load, loads due to hydrostatic pressure, the dead loads as a result of buoyancy and differential settlement effects.
- ii. Vertical live loads of HA or HB which acts on the carriageway/highway and includes cycle track loading, footway loading, accidental wheel loading and as well as construction traffic.<sup>11</sup> A formula for loading that represent normal traffic is referred to as HA loading while HB loading represent an abnormal

vehicle unit loading(according to Vincent T. H. Chu's "A self-learning manual mastering different fields of civil Engineering Works (VC-Q-A-Method)").

- iii. Horizontal live loads of surcharge, traction, temperature effects, parapet/head wall collision, accidental skidding and centrifugal load.

In general concerning culvert loading, B5400: part 2 1978 contains the requirement for culvert loading. The above are also contained in<sup>3</sup> Reinforced concrete design manual by Reynolds and Steelman's 1994 edition.

<sup>7</sup>The concept of type HA loads first came into awareness in the year 1945 while that of HB (highway bridges) loading was introduced in BS53 in the year 1954.

Type HA loads (normal traffic loading) covers vehicles up to 44 ton and are represented by uniformly distributed load with a knife edge load and:

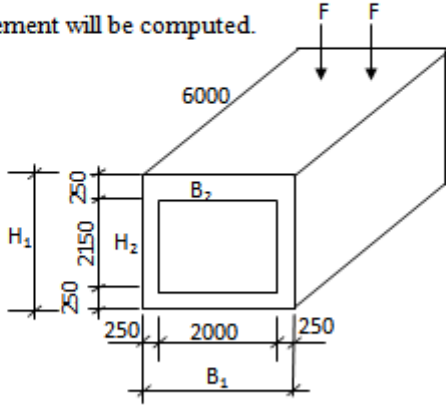
- a. Covers more than one vehicle occupying the width of a lane.
- b. Covers overloading in normal vehicles
- c. Covers impact load that are induced when car wheel bounce as at when travelling across potholes.

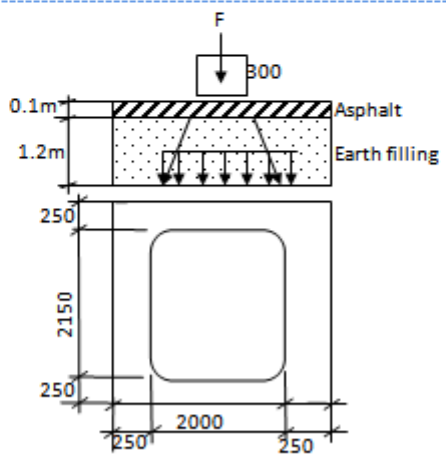
**TABLE 1: DESIGN INFORMATION**

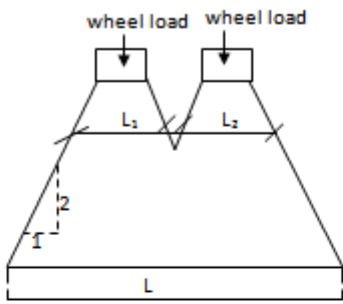
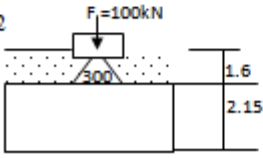
1.	Culvert sizing:	2000mm x 2150mm single cell in-to-in with 250mm uniform thickness of top slab, invert slab and walls with a total span of 6000mm
2.	Location:	Km 0 + 0.00 at Obibi drive Off Alaka Avenue, Etevie Community, Ozoro Delta State.
3.	Relevant Design Code:	i. BS5400: Part 2 1978 (load specification) ii. BS8110: Part 1: 1997 (Code of practice for design and construction) iii. Reinforced concrete designer's hand book (Reynold & Steelman)
4.	Soil Parametre:	Allowable bearing capacity; 200kN/m <sup>2</sup>
5.	Characteristic strength material data:	(i) Concrete f <sub>cu</sub> : 25N/mm <sup>2</sup> (ii) Main steel bars (f <sub>y</sub> ): 460N/mm <sup>2</sup> (iii) Distribution bars (f <sub>y</sub> ): 460N/mm <sup>2</sup>
6.	<b>General Loading Conditions</b>	
A.	<b>Dead load:</b> (i) Weight per m <sup>2</sup>	(i) Weight of concrete: 24kN/m <sup>2</sup> (ii) Weight of soil: 18kN/m <sup>2</sup> (iii) Weight of asphalt: 23kN/m <sup>2</sup> (iv) Weight of water: 10kN/m <sup>2</sup>
	(ii) Dead load Values of partial factor of safety BS5400-1	(i) Self weight of culvert: 1.15 (ii) Earth fill (earth pressure): 1.50 Asphalt: 1.00

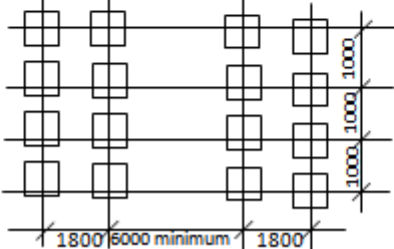
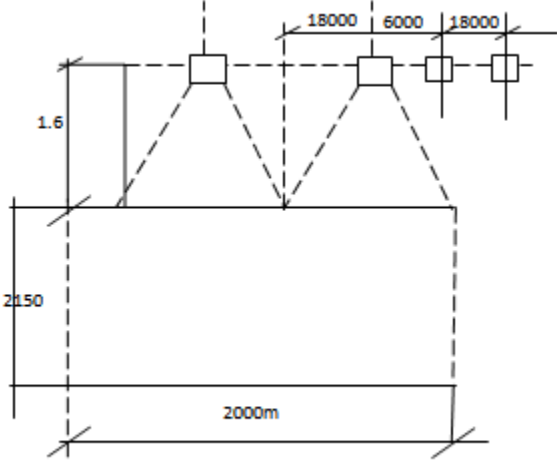
B	<p><b>Imposed load</b></p> <p>(i) Design HA loading combined with design HB 45 units loading</p> <p>(ii) Imposed load values of partial factor of safety</p>	<p>(i) <b>HA:</b> single wheel load of 100kN of square contact area of 300mm by 300mm of 1.1kN/mm<sup>2</sup> effective pressure.</p> <p>(ii) <b>HB:</b> a four axle vehicle of 10kN per axle, with four wheels equal spacing on each axle of 2.5kN per wheel of four wheel per axle of 45 units: HA (HB45)</p> <p>(i) HA vehicles (ULS) 1.50</p> <p>(ii) HB vehicles (ULS) 1.30 (SLS) 1.10</p>

**DESIGN OF BOX CULVERT**

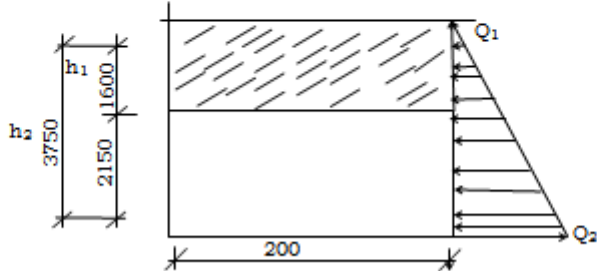
Ref	<p>In this paper, structural analysis and design of culvert with details as shown in figure 1 will be discussed and analyzed for maximum bending moment and maximum shear force caused by the result of the application of vehicle wheel load, hydrostatic pressure, earth pressure, and self-weight of the culvert after which the reinforcement will be computed.</p>  <p><b>Figure 1: Single Cell Culvert size details</b></p>	Output
	<p>From figure 1, effective depth:</p> $Deff = t - \text{Concrete cover} - \frac{\theta}{2}$ $\therefore deff = 250 - 50 - \frac{20}{2}$ $= 250 - 50 - 10$ $= 190\text{mm}$	<p>(where <math>\theta</math> is assumed diameter of rebar = 20mm)</p> <p>cover = 50mm</p> <p>(for severe conditions of exposure).</p>

<b>LOADING</b>		
	<p>(a) Dead load:</p> <p>(i) Top slab = <math>1.15 \times 24 \times 0.25</math></p> <p>(ii) Bollous slab = <math>1.15 \times 24 \times 0.25</math></p> <p>(iii) Walls = <math>1.15 \times 24 \times 0.25 \times 3 \times 2.15</math></p> <p>(iv) Weight of Asphalt = <math>1.0 \times 0.1 \times 23</math></p> <p>(v) Weigh of fill = <math>1.5 \times 1.6 \times 18</math></p> <p>Total dead load</p> <p>(b) Imposed load:</p>	<p>6.9kN/m<sup>2</sup></p> <p>6.9 kN/m<sup>2</sup></p> <p>44.51 kN/m<sup>2</sup></p> <p>2.3 kN/m<sup>2</sup></p> <p>43.2kN/m<sup>2</sup></p> <p>103.81kN/m<sup>2</sup></p>
<p>BS5400</p> <p>Part 2</p> <p>6.2.5</p> <p>6.2.6</p> <p>6.4.1.5</p>	 <p style="text-align: center;">Figure 2a: Wheel load dispersion on culvert</p>	<p>Cover depth &gt;0.6m</p> <p>HA</p> <p>UDL/KEL not applicable</p> <p>30 units of HB loading rules</p> <p>OR</p> <p>Wheelload dispersal on box culvert single</p> <p>100kNHA</p>

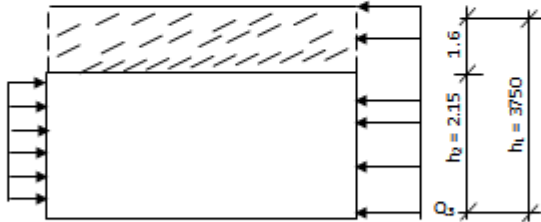
	 <p>Figure 2b: Wheel load dispersion on culverts diagram</p>	
	<p><b>CASE I: 100kN HA wheel load (stress due to HA vehicle)</b></p>	
<p>BS5400 Part 1 6.2.5 6.2.6 6.4.1.5 <a href="http://strudnle.com">http://strudnle.com</a></p>	<p>Single wheel load of 100kN @ 1.1N/mm<sup>2</sup> effective pressure will produce contact area (A<sub>CT</sub>):</p> $A_{CT} = \sqrt{\frac{100 \times 10^3}{1.1}} = 302 \times 302$  <p>Figure 3: Stress due to HA vehicle,</p>	
	<p>@ <math>\frac{2}{1}</math> gradient.</p> <p>Dispersal area to the top slab of the culvert (A<sub>dsp</sub>):</p> $\therefore A_{dsp} = A_{CT} + 2 \times \left( \frac{F_d}{2} \right)$ $= 302 + \left[ 2 \times \left( \frac{1600}{2} \right) \right]$ $= 302 + 1600 = 1902 \times 1902$ <p>@ top slab thickness = 250mm then neutral axis (F<sub>dsa</sub>) = 125mm (F<sub>dsa</sub>)</p> <p><math>\therefore</math> Dispersal width to neutral axis of culvert (W<sub>dsa</sub>)</p>	<p>A<sub>dsp</sub> = Dispersal area</p> <p>A<sub>CT</sub> = Contact area</p>

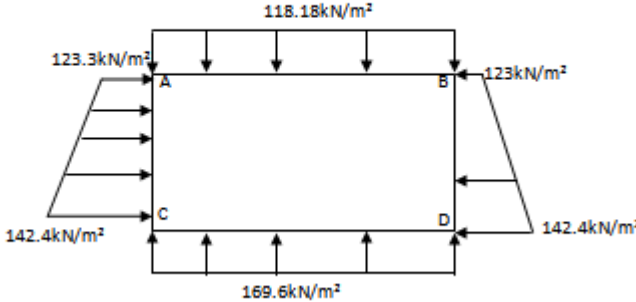
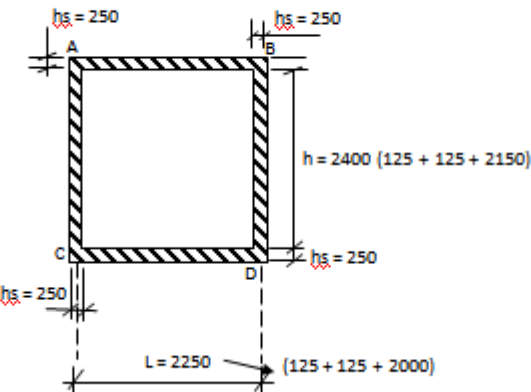
	<p>Thus <math>W_{dep} = A_{CT} + F_d + 2F_{des}</math></p> $= 302 + 1600 + 2(125)$ $= 2152mm$ <p>∴ wheel load (<math>F_{des}</math>) on dispersed area:</p> $F_{des} = \frac{100}{2.152 \times 2.152} = 21.6kN/m^2$	<p><math>F_d</math> = Fill depth</p> <p><math>F_{des}</math> = Neutral axis is at half <math>F_d</math>.</p>
<p><a href="http://strudrile.com">http://strudrile.com</a></p>	<p><b>CASE II: 45 units of HB Load (stress due to HB vehicle)</b></p> <p>Wheel load = <math>45 \times \frac{10}{4} = 1125kN</math></p> $A_{CT} = \sqrt{\frac{112500}{1.1}} = 320 \times 320mm$	
<p>BS5400 Part 2 6.3.1 6.3.2 6.3.3 Reynold T11</p>	 <p>Figure 4: The configuration of HB wheel load</p>	
	 <p>Fig 5: Stress due to HB vehicle</p>	

	<p>Total fill depth (<math>F_{ct}</math>): For neutral axis = <math>\frac{1}{2}</math> top slab thickness (250mm) provided the structure have no longitudinal joints.</p> $F_{ct} = F_d + F_{da}$ $= 1600 + \frac{250}{2} = 1600 + 125 = 1725\text{mm}$	
	<p>@ <math>\frac{1}{1}</math> gradient</p> <p>Transverse dispersal lines will overlap at a depth of:</p> $T_{dd} = 1000 - 320$ <p>(4 wheels on each axle at a spacing of 1000mm for HB loading figure 5) <math>T_{dd} \rightarrow</math> Transverse dispersal depth</p> $= 680\text{mm} < 1650\text{mm} \rightarrow (\text{ok, 4 wheels considered})$ <p><math>\therefore</math> Total width that an axle will dispersed (<math>T_{wad}</math>):</p> $T_{wad} = A_{CT} + (n-1)S + F_d + F_{da}$ <p>Where:</p> $T_{wad} = 320 + (4 - 1) 1000 + 1600 + 2 (125) = 5170\text{mm}$	<p><math>T_{dd} =</math> Transverse dispersal dept</p> <p>T = total w = width a = axle d = disperse n = number of axles s = spacing c/c of axle 250</p>
	<p>Or <math>T_{wad} = 3000 + 320 + \left(2 \times \frac{1600}{2}\right) + \left(2 \times \frac{250}{2}\right)</math></p> $= 5170\text{mm (from figure 6)}$	
	<p>@ <math>\frac{1}{1}</math> gradient</p> <p>Longitudinal dispersal liens overlaps at a depth of:</p> $L_{dd} = 1800 - 320$ <p>(front and rear pair of axles are spaced at 18000)</p> $= 1480 < 1650\text{mm (ok, front and rear pair of axles are considered)}$ <p><math>\therefore L_{dd} = A_{CT} + (n - 1)S + F_d + 2F_{da}</math> (<math>L_{dd}</math> = longitudinal</p>	<p><math>L_{dd} =</math> Longitudinal dispersal dept</p>

<p>BS5400 Part 2 6.2.7</p>	<p>dispersal depth)  <math>= 320(z - 1) 1800 + 1600 + 2(125)</math>  <math>= 320 + 1800 + 1600 + 250 = 3970\text{mm}</math>  <math>\therefore</math> the axle load on dispersal area of top slab of culvert (<math>F_{da}</math>);  <math display="block">F_{da} = \frac{N_w \times W_f}{A_d}</math>  <math display="block">\Rightarrow F_{da} = \frac{8 \times 1125}{5.170 \times 3.970} = 43.85\text{kN/m}^2 &gt; 21.6\text{kN/m}^2</math>  <math display="block">\Rightarrow 43.85 \times 1.5 &gt; 21.6 \times 1.5</math>  <math display="block">= 65.78\text{kN/m}^2 &gt; 32.4\text{kN/m}^2</math>          Thus between case I and case II, case II is critical @  <math>43.85\text{kN/m}^2 &gt; 21.6\text{kN/m}^2</math>  <math>\therefore</math> UDL acting on top of the culvert that is appropriate for the          design = <math>43.85\text{kN/m}^2</math></p>	<p><math>N_w</math> = number of wheel  <math>W_f</math> = wheel load  <math>A_d</math> = dispersal area  <math>F_{da}</math> = axle load for F = load d          = dispersal a = axle</p>
<b>ACTIVE EARTH PRESSURE ON WALLS</b>		
<p>BS54000 Part 2 5.81 Reynold T16</p>	<p>Let active earth pressure = K  <math display="block">k = \frac{1 - \sin\theta}{1 + \cos\theta}, \theta = 30^\circ</math> (angle of slope of bank of retained material)  <math>K = 0.333</math></p>  <p>Figure 6: Active pressure on vertical wall of culverts</p>	



	$Q_2 = Kh_2 p 1.5 = 0.33 \times 3.75 \times 18 \times 1.5 = 33.4 \text{ kN/m}^2$ $Q_1 = Kh_1 p 1.5 = 0.33 \times 1.6 \times 18 \times 1.5 = 14.3 \text{ kN/m}^2$ <p><b>HYDROSTATIC PRESSURE ON INVERT FLOOR</b></p> $\rho_w = 9.801 \text{ kN/m}^3 \approx 10 \text{ kN/m}^3$ $h_2 = 2.15 \text{ m (@ a maximum flooring of 2.15 m at peak period that culvert is full of water)}$ $\therefore P_{HY} = P_w \Rightarrow \text{hydrostatic pressure}$ $\Rightarrow \rho_w h = \rho_w H = 10 \times 2.15 = 21.5 \text{ kN/m}^2$	
	<p><b>SURCHARGE PRESSURE ON CULVERT WALLS</b></p>  <p>Figure 7: Surcharge pressure on walls</p> $Q_3 = K(F_{da} + N_{FL})$ $= 0.33 \times (43.85 + 43.2)$ $\therefore Q_3 = 0.33 (43.85 \times 1.5) + 43.2$ $= 108.0 \text{ kN/m}^2$	$Q_3 = \text{surcharge pressure}$ $F_{da} = \text{load dispersal due to axle of vehicle on walls}$ $N_{FL} = \text{weight of fill on walls}$
	<p><b>CHECK FOR ADEQUACY OF SOIL BEARING CAPACITY</b></p> <ol style="list-style-type: none"> <li>i. Allowable soil bearing capacity = 200 kN/m<sup>2</sup></li> <li>ii. Total design load on the soil = Dead load + imposed load</li> </ol> $= 11.35 \times 103.81 + 43.85 \times 1.5$ $= 146.1435 + 65.775$ $= 206 \text{ kN/m}^2 > 200 \text{ kN/m}^2$	

	<p style="text-align: center;"><b>TOTAL BENDING PRESSURE ON CULVERT MEMBERS</b></p>  <p>Figure 8: Bending pressures on culvert members (total)</p> <p>Top slab = (slab wt. + fill wt + Asphalt wt + HB)  <math>= 6.9 + 43.2 + 2.3 + 65.78 = 118.18 \text{KN/m}^2</math></p> <p>Bottom slab = Top slab wt + invert slab wt + walls wt  <math>118.18 + 6.9 + 44.51 = 169.59 \text{KN/m}^2</math></p> <p>Side walls:</p> $Q_1 = Q_1 + \text{surcharge pressure}$ $= 14.3 + 109 = 123.3 \text{KN/m}^2$ $Q_2 = Q_2 + \text{surcharge pressure}$ $= 1334 \text{KN/m}^2 + 109 \text{KN/m}^3 = 142.4 \text{KN/m}^2$	
<p>Reynold &amp;  steelman page  473 T 187</p>	<p style="text-align: center;"><b>BENDING MOMENTS PER UNIT LENGTH OF CULVERT</b></p> 	<p>(i) Rectangular box culvert  (ii) highly compressible soil  (iii) <math>M_A = M_B, M_C = M_D</math></p>

	<p>Figure 9: culverts (sizes) measurement</p> <p>From figure 9, <math>k = \frac{h}{l} \left( \frac{hs}{hw} \right)^2 = \frac{2.4}{2.25} \left( \frac{25}{25} \right)^2 = 1.1</math></p>	
<p>Reynold and steelman T187 page 473</p>	<p>K coefficient values computation</p> <p>From K = 1.1;</p> <p>(1) <math>k_1 = k + 1 = 2.1</math>  (2) <math>k_2 = k + 2 = 3.1</math>  (3) <math>k_3 = k + 3 = 4.1</math>  (4) <math>k_4 = 4k + 9 = 13.4</math>  (5) <math>k_5 = 2k + 3 = 5.2</math>  (6) <math>k_6 = k + 6 = 7.1</math>  (7) <math>k_7 = 2k + 7 = 9.2</math>  (8) <math>k_8 = 3k + 8 = 11.3</math></p>	
<p>Reynold &amp; steelman T197 page 473</p>	<p>Bending moments</p> <p>1. UDL on top slab, <math>Q = 118.8 \text{ kN.m}^2</math></p> <p>Moment due to UDL load on top slab</p> <p>For <math>\bar{M}_A = \bar{M}_C = \frac{QL^2}{12k_1} = \frac{118.8 \times 2.25^2}{12 \times 2.1} = -24 \text{ kN-m}</math></p> <p>2. Weight on bottom/invert slab (and the water in the culvert) are directly carried by the ground underneath the invert slab</p> <p><math>\therefore</math> moment due to load on bottom slab = 0kN-m</p> <p>3. Moment as a result of weight of vertical walls</p> <p>i. <math>Q_1 = \frac{2G}{1+hw} = \frac{2 \times 44.51}{1.25} = 71.2 \text{ kN/m}^2</math></p> <p>ii. Moment due to <math>Q_1</math> in 3(i)</p> <p><math>\bar{M}_A = \frac{Q_1 L^2 k}{12k_1 k_3} = \frac{71.2 \times 2.25 \times 1.1}{12 \times 2.1 \times 4.1} = 1.71 \text{ kN-m}</math></p> <p><math>\bar{M}_C = \frac{k_3}{k} \bar{M}_A = \frac{5.2}{1.1} \times 1.71 = -8.1 \text{ kN-m}</math></p>	

	<p>4. moment as a result of earth pressure on walls:</p> $Q_2 = 33.4 \text{KN/m}^2$ $\bar{M}_A = \frac{Q_2 h^2 k_1 k_2}{60 k_1 k_3} = \frac{33.4 \times 2.40^2 \times 1.1 \times 9.2}{60 \times 1.1 \times 4.1}$ $= -7.1 \text{KNm}$ $\bar{M}_C = \frac{k_1}{k_3} M_A = \frac{11.3 \times 7.1}{9.2} = 8.7 \text{KN-m}$	
	<p>5. Moments due to earth surcharge pressure on vertical wall</p> $Q_3 = 109 \text{KN/m}^2$ $\bar{M}_A = \bar{M}_C = \frac{Q_3 h^2 k_1}{12 k_1} = \frac{109 \times 2.46^2 \times 1.1}{12 \times 2.1} = -27 \text{KN-m}$	
	<p>6. Moment due to hydrostatic internal pressure; <math>p_{hy} =</math> hydrostatic pressure = 21.5kn/m<sup>2</sup> =</p> $\bar{M}_A = \frac{p_{hy} h^2 k_1 k_2}{60 k_1 k_2} = \frac{21.5 \times 2.40^2 \times 1.1 \times 2.1}{60 \times 2.1 \times 3.1} = 0.73$ $\bar{M}_C = \frac{k_1}{k_3} M_A = \frac{11.3}{9.2} \times 0.73 = 0.90 \text{KN-m}$	
	<p>7. Moment due to excess hydrostatic internal pressure</p> $P_{hy} = Q_{e0} = 21.5 \text{KN/m}^2$ $\bar{M}_A =$ $\frac{Q_{e0} p (h^2 k_1 + L^2 k_2)}{12 k_1 k_2} = 21.5 \left[ \frac{2.40^2 \times 1.1 \times 4.1 + (2^2 \times 4.1)}{12 \times 2.1 \times 4.1} \right] = 9.21 \text{KN-m}$ $\bar{M}_C = \frac{Q_{e0} K (h^2 k_1 - L^2)}{12 k_1 k_2} = \frac{21.5 \times 1.1 [2.45 \times 4.1 - 2^2]}{12 \times 2.1 \times 4.1}$ $= 4.44 \text{KN-m}$	

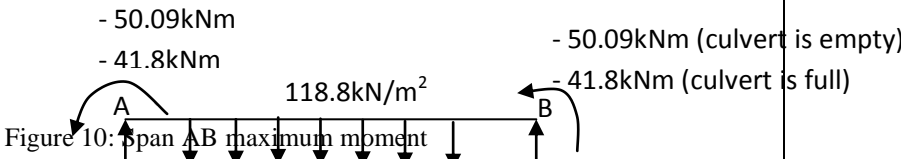
TABLE 2: BENDING SUPPORT MOMENTS PER UNIT LENGTH OF CULVERT SUMMARY

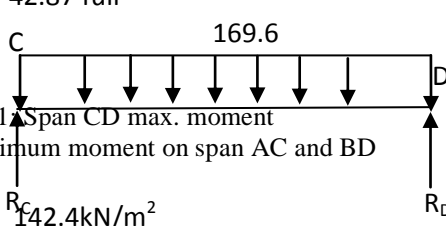
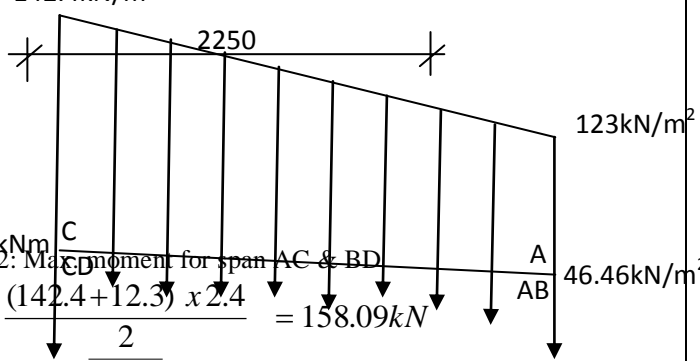
S/N	Loading	Ma=MB	Mc=MD	Remarks
1.	UDL on top slab: 118.18KN/m <sup>2</sup>	-24KN-m	-24KN-m	M <sub>A</sub> = M <sub>B</sub> = M <sub>C</sub> = M <sub>D</sub>
2.	Weight of walls on culvert: 71.2KN/m <sup>2</sup>	+1.71KN-m	-8.1KN-m	M <sub>A</sub> = M <sub>B</sub> M <sub>C</sub> = M <sub>D</sub>
3.	Earth pressure on walls 33.4KN/m <sup>2</sup>	-7.1KN-m	+8.7KN-m	M <sub>A</sub> = M <sub>B</sub> M <sub>C</sub> = M <sub>D</sub>
4.	Earth surcharge pressure on walls 109K/m <sup>2</sup>	-27KN-m	-27KN-m	M <sub>A</sub> = M <sub>B</sub> = M <sub>C</sub> = M <sub>D</sub>
	<b>Total if culvert is empty</b>	<b>-56.39KN-m</b>	<b>-50.4KN-m</b>	<b>Culver is without water</b>

5.	Hydrostatic internal pressure: 21.5KN/m <sup>2</sup>	+0.73KN-m	+0.98KN-m	M <sub>A</sub> = M <sub>B</sub> M <sub>C</sub> = M <sub>D</sub>
6.	Excess hydrostatic internal pressure 21.5KN/m <sup>2</sup>	+9.21KN-m	+4.44KN-m	M <sub>A</sub> = M <sub>B</sub> M <sub>C</sub> = M <sub>D</sub>
	<b>Total if culvert is full</b>	<b>-46.46KN-m</b>	<b>-44.98KN-m</b>	<b>Culvert is full with water</b>

**MAXIMUM SPANS MOMENTS**

Span moment will be computed for AB, CD, AC, and BD

<p>Reff: Mosely, Bungey and hulse 7<sup>th</sup> edition</p>	<p>i. Maximum span moments of AB</p> <p>(a) <math>R_A = \frac{wl}{2} = \frac{118.18 \times 2.25}{2} = 132.96KN</math></p> <p><math>R_B = 132.96kN</math></p> <p>(b) Distance to zero shear <math>\Rightarrow \chi</math></p> $\chi = \frac{R_A}{w} = \frac{132.96}{118.18} = 1.13m$ <p>(c) maximum span moment (M<sub>max</sub>) will occur at zero shear, Thus at <math>\chi = 1.13m</math>,</p> <p>(i) <math>M_{\max(\text{full})} = \frac{R_A^2}{2w} + M_A</math> (culvert is full)</p> $= \frac{132.96^2}{2 \times 118.18} + (-46.39)$ $= \frac{132.96^2}{2 \times 118.18} + (-46.46) = 28.33KN - m$ <p>(ii)</p> $M_{\max(\text{empty})} = \frac{132.96^2}{2 \times 118.18} + (-56.36) = 18.4KN$ (culvert is empty) <div style="text-align: center;">  </div> <p>(ii) maximum movement on span CD</p> <p>(a) <math>R_C = \frac{wl}{2} = \frac{169.6 \times 2.25}{2} = 190.8kN = R_D</math></p> <p>(b) Distance to zero shear <math>\Rightarrow x</math></p> $x = \frac{R_C}{w} = \frac{190.8}{169.6} = 1.13m$ <p>(c) Maximum span moment (M<sub>max</sub>) will occur at zero shear</p>	<p>- 50.09kNm (culvert is empty)</p> <p>- 41.8kNm (culvert is full)</p>
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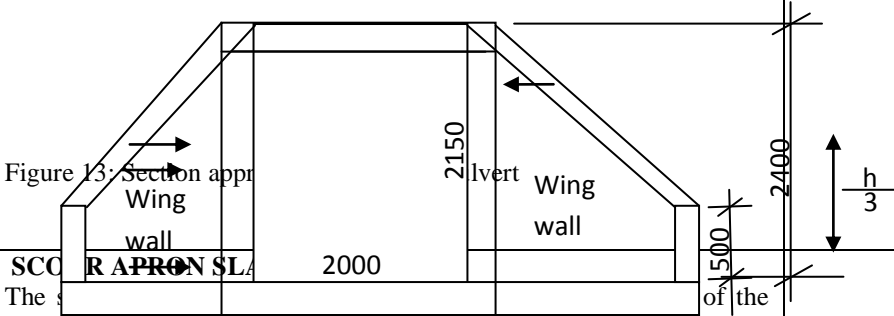
	<p>(i) <math>M_{\max(\text{full})} = \frac{R_c^2}{2w} + M_c</math> (culvert is full)</p> $= \frac{190.8^2}{2 \times 169.6} + (-46.46) = 56.93 \text{ kNm} = 60.9 \text{ kN-m}$ <p>(ii) <math>M_{\max(\text{empty})} = \frac{190.8^2}{2 \times 169.6} + (-50.4)</math> (culvert is empty)</p> $= 56.93 \text{ kN-m}$ <p>- 47 empty - 42.87 full</p> <p style="text-align: right;">- 47 empty - 42.87 full with water</p>  <p>Figure 11: Span CD max. moment</p> <p>(iii) maximum moment on span AC and BD</p>  <p>Figure 12: Maximum moment for span AC &amp; BD</p> <p>(a) <math>R_A = \frac{(142.4 + 12.3) \times 2.4}{2} = 158.09 \text{ kN}</math></p> <p>(b) distance to zero shear</p> $\chi = \frac{R_A - w}{w} = \frac{158.09 - 319.807}{319.807} = 0.494 \text{ m}$ <p>(c) (i) <math>M_{\max(\text{full})} = \frac{161.717}{2 \times 319.807} - 46.46 = -5.57 \text{ kNm}</math> (culvert is full)</p> <p>(ii) <math>M_{\max(\text{empty})} = \frac{161.717}{2 \times 319.807} - 56.39 = 15.5 \text{ kNm}</math> (culvert is empty)</p>	
<p>Mosley Bungey Hulse</p>	<p><b>DESIGN WING WALL</b></p> <p>Wing walls prevent scour effects, soil erosion, retains the embankment and directs water flow. Earth pressures from the back fill material, surcharge pressure from live load or compacting machine and hydraulic loads from saturated seal conditions are all design considerations. Also to be considered in the design of wing wall is the lateral earth and surcharge pressure factors.</p> <p>Lateral earth pressure factor = 1.35 <math>\Rightarrow \gamma \tau</math></p> <p>The horizontal force (F) due to earth pressure is given by:</p>	

$F = \gamma \tau 0.5K\alpha h^2$   
 $= 1.35 \times 0.5 \times 33 \times 18 \times 2.4^2 = 23.1 \text{ kN}$

This force is acting approximately @  $\frac{h}{3}$  from the base apron of wingwall.

Thus for F, acting at  $\frac{h}{3}$  from base of wall;

$\therefore \text{Moment, } M = F \times \frac{h}{3}$   
 $= 23.1 \times \frac{2.4}{3}$   
 $= 20.53 \text{ kNm}$



**SCOUR PROTECTION**  
 The apron slab is provided at the base of the culvert and it is designed to protect and prevent the culvert from scour, storm damage and erosion damage of the base apron.

There is an upward pressure (Q) at the base of the bottom slab (figure 13).  
 $Q = \text{self-weight of the apron slab itself} = 0.25 \times 24$   
 $= 6 \text{ kN/m}^2 \text{ per linear metre}$

$\therefore M = \frac{QL^2}{8} = \frac{6 \times 6}{8} = 27 \text{ kNm}$

**TABLE 3: DESIGN RESULT SUMMARY**

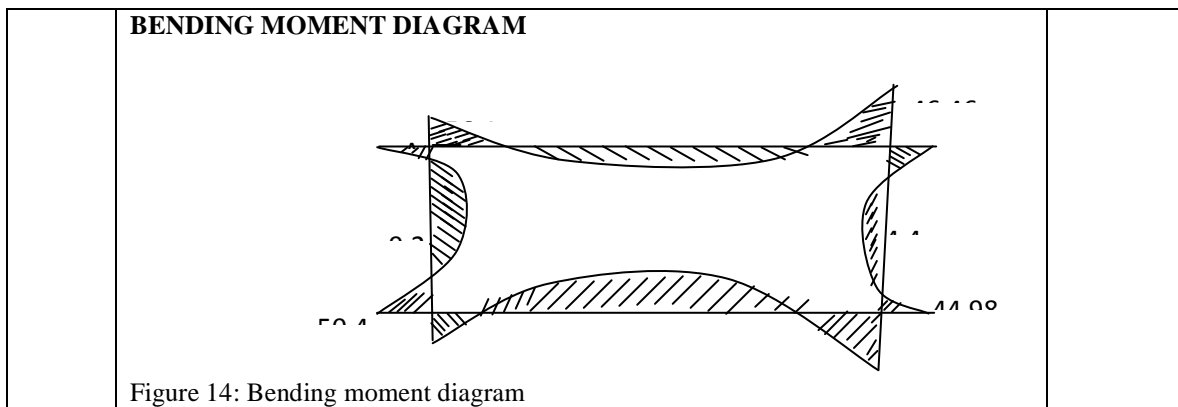
S/no	Culvert component	Moment (kN-m)		K		Z = d [ 0.5 + √(0.125 + 0.000125 M / (b d^2 F <sub>cu</sub> )) ]		As <sub>req</sub> = $\frac{M}{0.87 f_y z}$		As provided
		Support	Mids pan	Support	Mids pan	support	Midspan	support	Mids pan	
1.	Top slab (a) culvert is full	-46.46	28.33	0.051		181		641		Y16 mmθ @ 200 c/c 1010mm <sup>2</sup>
	(b) culvert is empty	-56.39	18.4							
2.	Bottom slab (i)	-44.98	60.9		0.07		177		850	Y16 mmθ @ 150 c/c

	culvert is full (ii) culvert is empty	-50.4	56.9 3	0.05 6						1340mm <sup>2</sup>
3.	Side walls weight (i) culvert is full (ii) culverts is empty	-46.46  -56.39	-5.57  -15.6							
4.	Earth pressure on walls (i) full (ii) culvert is empty	-46.46  -56.39	-  -							
5.	Earth surcharge pressure	44.48 56.38	-							
6.	Hydrastic pressure internal pressure	-44.98	-							Y10 mmØ @ 200 c/c 393 mm <sup>2</sup>
7.	Excess hydrastic internal pressure	-44.98 -50.4	-							
8.	Wing wall	-	20.5 3	0.02 2		186		276		
	Apron slab	-	27		0.03	184		367		Y12 mmØ @ 200 c/c 566 mm <sup>2</sup>
9.	Distribution bars		$\text{Area of steel} = 0.13\% bh = \frac{0.13 \times 190 \times 1000}{100} = 247\text{mm}^2$							Y10 mmØ @ 200 c/c 393 mm <sup>2</sup>
	Mosley Bungey & hulse table 6.10	<p><b>CHECKING FOR SAFETY OF THE DESIGN</b></p> <p>(a) Check span – effective dept ratio:</p> <p>The steel ratio <math>\rho</math>, is defined as; <math>\rho = \frac{100A_{sreq}}{bd}</math></p> <p>When <math>\rho &gt; 1.5\%</math>: the level of concrete stress under serviceability condition is highly stressed</p> <p>When <math>\rho = 0.5\%</math>: the level of concrete stress under serviceability condition is lightly stressed</p>								



	<p>Hence <math>\rho = \frac{100 \times 850}{1000 \times 190} = 0.447 \approx 0.5\%</math> (hence <math>\rho</math> is lightly stressed and <math>&gt;0.13\%</math> minimum ok)</p> <p>Basic span – effective dept, ratio = 24 For <math>f_y = 460</math> is <math>&lt; 500</math></p> <p>Thus basic span – effective dept ratio = <math>24 \times \frac{500}{460} = 26</math></p> <p>(i) <math>\text{actual} = \frac{\text{Span}}{\text{effective dept}} = \frac{2250}{190} = 11.84</math></p> <p>Limiting <math>\frac{\text{Span}}{\text{eff. dept}} \Rightarrow \text{basic ratio} \times \frac{A_{sprov}}{A_{srq}}</math></p> <p><math>= 26 \times \frac{1010}{850} = 26 \times 1.2 = 31.2 &gt; 11.84, \text{ok}</math></p> <p>Hence</p> <p>(ii) <math>\frac{\text{Allowable span}}{\text{effective dept}} = 31.2 &gt; \frac{\text{actual span}}{\text{effective}} = 11.84</math></p> <p><math>\therefore</math> effective dept = 190mm is adequate and acceptable</p>
<p>B58001 Part 1:3.4.4.4( b)</p>	<p><b>CHECK FOR DEFLECTION</b></p> <p>For deflection check; modification factor (<math>M_f</math>) = <math>\frac{0.55 + 477 - f_s}{120(0.9 + \frac{M}{bd^2})} \leq 2.0</math></p> <p>But <math>f_s = \frac{2}{3} f_y \frac{A_{srq}}{A_{sprov}} \left(\frac{1}{\beta_1}\right) \beta_1 = 1</math> (where redistribution is not required)</p> <p><math>M_f = \frac{0.55 + 477 - 258.1}{120(0.9 + 1.7)} = \frac{219.55}{315} = 0.7 &lt; 2.0, \text{ok}</math></p> <p>From <math>M_f = 0.7</math> and Basic span – effective dept ratio = 26 <math>\therefore</math> limiting <math>M_f</math> value = <math>0.7 \times 26 = 18.2</math> But:</p> <p>Actual <math>\frac{\text{span}}{\text{effective dept}}</math> Value <math>\frac{2250}{190} = 11.84 &lt; 18.2</math></p> <p>Thus limiting value <math>&gt;</math> actual value: <math>18.2 &gt; 11.84, \text{ok}</math> And</p> <p>d required = <math>\frac{\text{span}}{2 \times \frac{\text{span}}{\text{eff. dept}} \text{ ratio}} = \frac{2250}{2 \times 26} = 43.3\text{mm} &lt; 190\text{mm ok}</math></p> <p><math>\therefore</math> deflection check is satisfied ok</p>
<p>Mosely Bungey Hulse B58110 – 1:1997</p>	<p><b>(C) CHECK FOR SHEAR REQUIREMENT</b></p> <p>For <math>V_u</math> = the ultimate shear force <math>V_s</math> = the shear stress (shear reinforcement)</p> <p><math>V_u = \frac{V_s}{bd}</math></p>

<p>Clause 3:4:5.12 B58110-1:1985 Clause 3.4.4.4</p>	<p><math>V_c =</math> ultimate concrete shear resistance</p> $V_c = \frac{100A_s p}{bd}$ <p><math>V_u &lt; V_c</math>, shear reinforcement not required</p> $V_u = \frac{V_s}{bd} = \frac{190.8}{1000 \times 190} = 0.001$ $V_c = \frac{100 \times 1010}{1000 \times 190} = 0.53 > V_c = 0.001$ <p><math>\therefore</math> shear reinforcement is not required (<math>V_u - V_c</math>, ok)</p>
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**CONSTRUCTION OF CULVERTS**

<sup>1</sup>Service life of culverts should equal the service life of the highway hence a culvert should be designed and constructed to equal the service life of the structure it is serving.

There are reasons why culverts can <sup>1,7,9</sup>fail, reasons such as poor or no maintenance, environmental conditions, improper and non-engineering compliance during construction and structural failure leading to collapse or erosion. Therefore, to avoid and prevent failure, accurate engineering design and construction methods consideration should be a priority.

<sup>1</sup>Economic analysis and consideration in the design and construction of culvert include an economic analysis such as construction cost factors amongst others.

Culvert location should be an economical and effective need for usage. Location must be where construction is convenient for construction and in a location where required gradient must be achieved.

**BENEFIT TO HUMANITY**

<sup>1,9,7</sup>Culvert functions range from hydraulic and structural safety performance such as provision of cross drainage for stream channel, flood plain relief drainage during flood periods, and non-

hydraulic function such as acting as a crossing structure for humans/animal traffic as in pedestrian crossing, vehicles and rails crossing and cow and other animal's crossing. <sup>7, 1</sup>These functions of culvert benefit human in decreasing traffic interruption period as a result of road route flooding including the increasing confidence of safe driving.

**II. CONCLUSION AND RECOMMENDATION**

The dimension of the culvert were chosen to suit its location on site and is designed as a single cell with a total length of 6m and a total width of 2m in-to-in, 2.25m centre to centre span with its vertical side walls being 2.4m centre to centre but with in-to-in 2.15m height. The thickness of the culvert is 0.25m for all its structural element members. The single cell box culvert was analysed and designed for the maximum bending moment and shear force in each of the structural element members. The reinforcement provided are: Y16mm $\theta$  @ 200 centre-to-centre for top slab, bottom slab, wing walls and vertical side walls. Y12mm $\theta$  @ 200 c/c for apron slab floor and distribution bars.

The results were checked for;

1. Span-effective depth ratio to ascertain adequacy of effective depth,
2. Modification factor to confirm deflections check is satisfied and
3. Shear force, to establish whether there is need for shear reinforcement.

This treatise also discussed requirements for box culvert construction.

In using the manual computation method, the various codes for reinforced concrete design were made use of (such as BS5400, BS8110) including other relevant design manuals such as Reynold and Steelman.

Based on the accurate/precise results using manual calculation for maximum bending moment, shear force and reinforcement bars, it is recommended that any engineer that will opt for software analysis must be experienced in manual computation of the analysis and design for maximum bending moment and shear force because it is what you feed into the computer that will bring expected result.

### III. CONTRIBUTION TO KNOWLEDGE

1. The developed unique approach use to present results of analysis and design for Bending Moments, shear forces and reinforcements as shown in table 2 and table 3 is a new concept researchers, practicing engineers and students will find useful and thereby contributing to knowledge.
2. The manual method of designing a culvert as it is done in this article is new to many engineers. Therefore, this work will act as a reference bench work for literature review, hence becoming a document that will continuously contribute to knowledge.
3. This work has contributed to knowledge by the awareness this work has created for the need of manual approach method in the analysis and design of box culvert.
4. This study for the first time ever has provided manual method of analyzing, computing and designing supports, maximum bending span moments, shear forces and reinforcement bars model options for civil engineering works.

5. There is a revelation of previously latent issues in an otherwise known and established problem as is clearly demonstrated in the use of tables to present results and in the method for the analysis of HA and HB loads.

### REFERENCES

- [1]. A. M. Mohammed (2018); Design of a Box Culvert: Re public of Iran, Al-mansor University College, Civil Engineering Department.
- [2]. B. Mosley, J. Bungey, R. Hulse; Reinforced Concrete Design (2014) Book Power (formely ELST) with Palgrave Macmichorn Seventh Edition (2014).
- [3]. C. E. Reynolds, J. C Steedman; Reinforced Concrete Designer's Handbook (Ninth edition, 1994); A view point publications.
- [4]. <https://civiltoday.com/construction/bridge/11-6-typesofculvert><http://structville.com>
- [5]. P. A. Creamer (2007) "Culvert Hydraulics; Basic Principle", Proffromonal Development Services (FDF), COWTECH Bridge Solutions Inc., Ohio
- [6]. P. L. Krishna, K. Rajasekhar; Analysis and design of Box Culvert (2018): International Journal of Science Technology & Engineering (IJSTE) Volume 4, Issue 10.
- [7]. Relevant Design Codes: BS5400 Part 2 1978, BS8119 Part 1.
- [8]. R. Patel, S. Jamle (2019); Analysis and Design of Box Culvert; A Manual Approach. International Journla of Advanced Engineering Research and Science (IJAERS) volume 6, Issue 3.
- [9]. Samaila Consultants, Consulting Engineers & Partners: <https://www.scribd.com>
- [10]. V. T. H. Chu; A self-learning manual mastering different fields of civil engineering works; VC-Q-A-Method.



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